

Fermion Mediated Interactions between Bosons in a Bose-Fermi mixture



*Chicago
downtown*

Cheng Chin

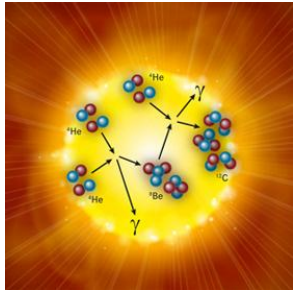
**Horace B. Horton Professor
James Franck institute
Enrico Fermi institute
Department of Physics
University of Chicago**



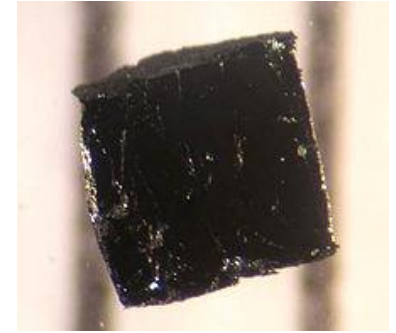
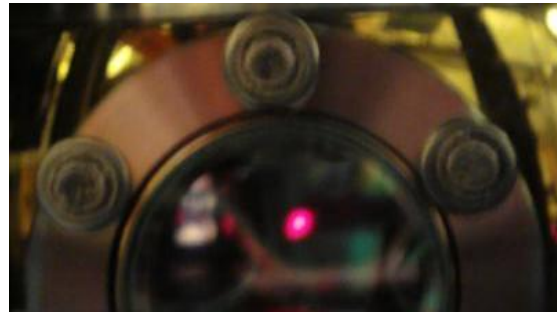
Quantum Simulation with Cold Atoms



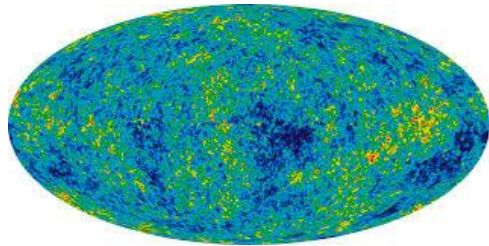
THE UNIVERSITY OF
CHICAGO



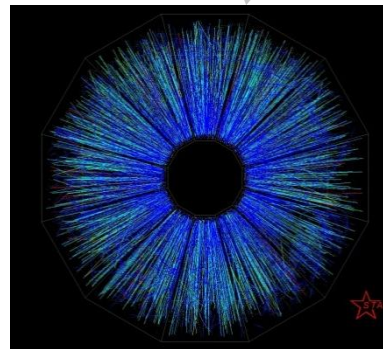
Nuclear Physics:
Feshbach resonance
Efimov physics



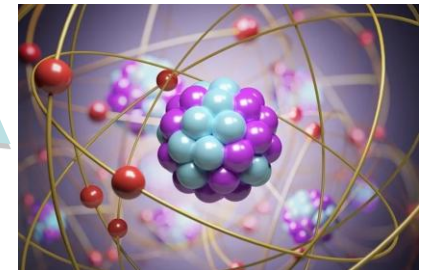
Condensed Matter:
RKKY interactions
Dynamical gauge field
Bilayer optical lattices



Cosmology and gravity
Kibble-Zurek mechanism
Inflation dynamics
Unruh radiation



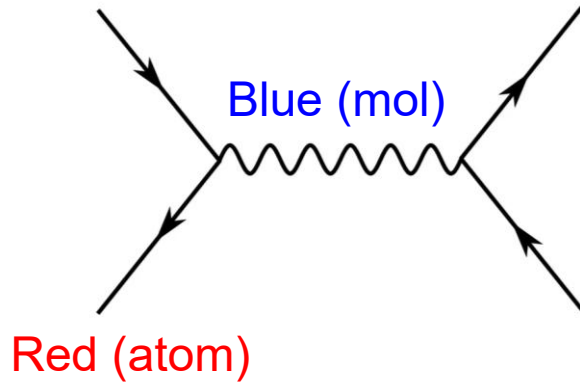
Jet Physics
Bose firework
HHG in BEC
Sub-jet structure
Pattern formation



Chemistry
Molecular BEC
Bose-enhance reaction
Phase doubling

Interactions generate entanglement

Red (atom)



Feshbach resonance $m^+ a_1 a_2 + H.c.$

Quantum optics $a_b^+ a_r a_r + H.c.$

HEP $\bar{\psi} \gamma^\mu \psi A_\mu + H.c.$

...

Key features:

Cosmology

- Inflation
- Unruh radiation

Material

- Pairing
- Quasi-particles

Optics

- Entanglement
- Two-mode squeezing

Chemistry

- Collective Reactions

Normal vs Many-body Chemistry

Normal Chemistry

Example: $2H \rightarrow H_2$

Reaction rate

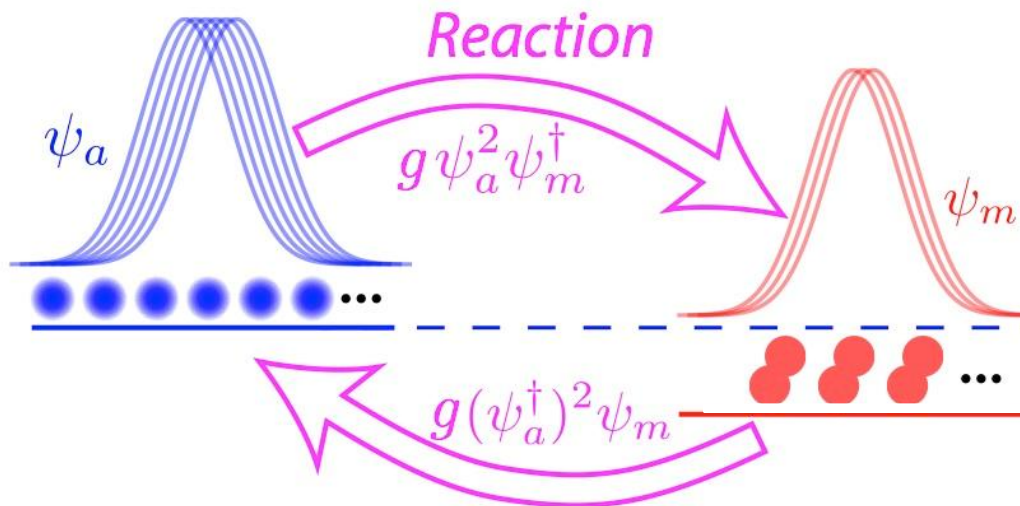
$$\Gamma = \sigma_r v [H]$$

Many-body Chemistry

$$\hat{V}_{int} = g\hat{\psi}_m^\dagger\hat{\psi}_a\hat{\psi}_a + g\hat{\psi}_m\hat{\psi}_a^\dagger\hat{\psi}_a^\dagger$$

$\hat{\psi}_m$: Molecular wave

$\hat{\psi}_a$: Atomic wave



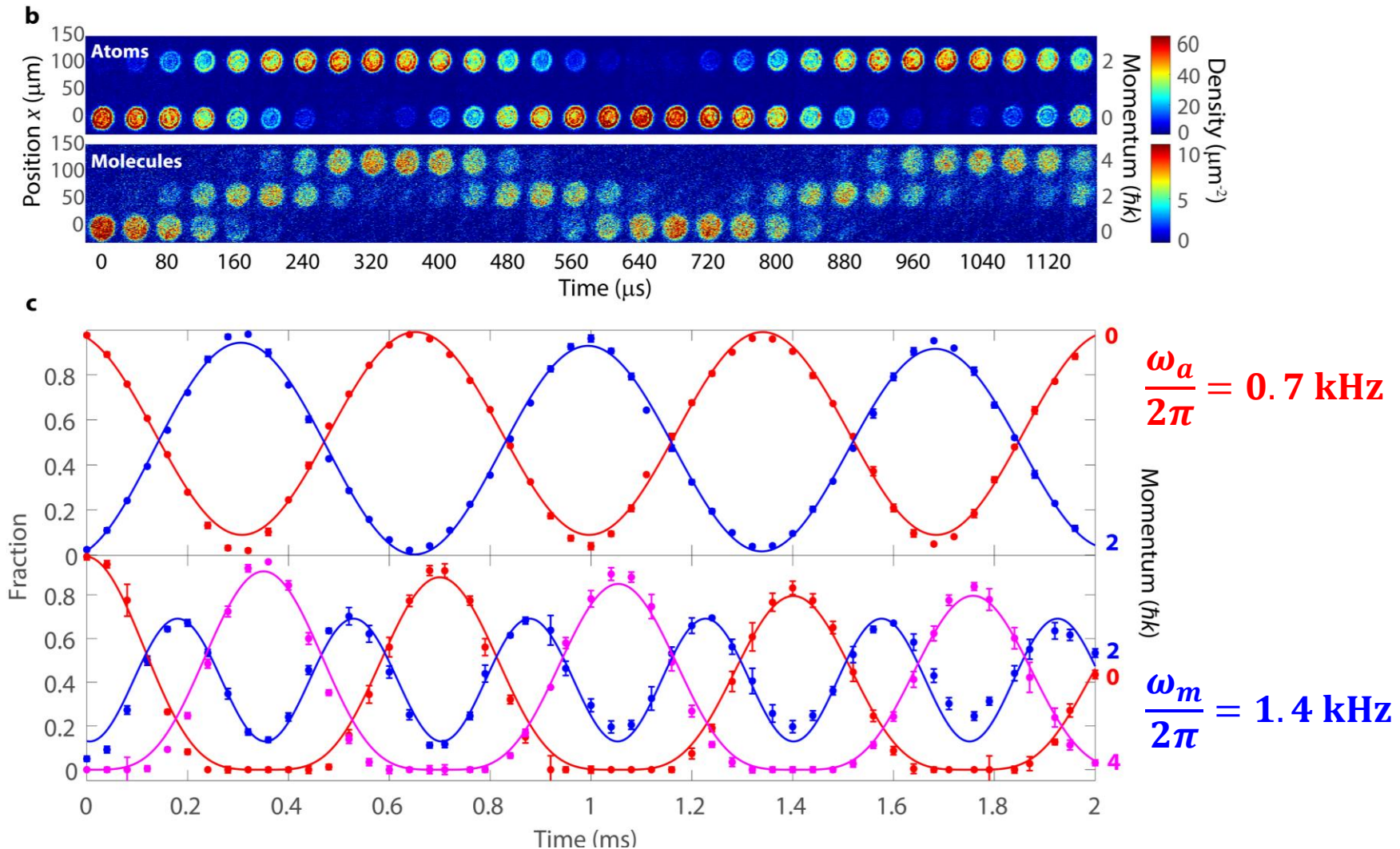
Features of Super-chemistry

- A.-M. BEC coupling
- Bose enhanced reaction
- Phase matching
- Entanglement generation

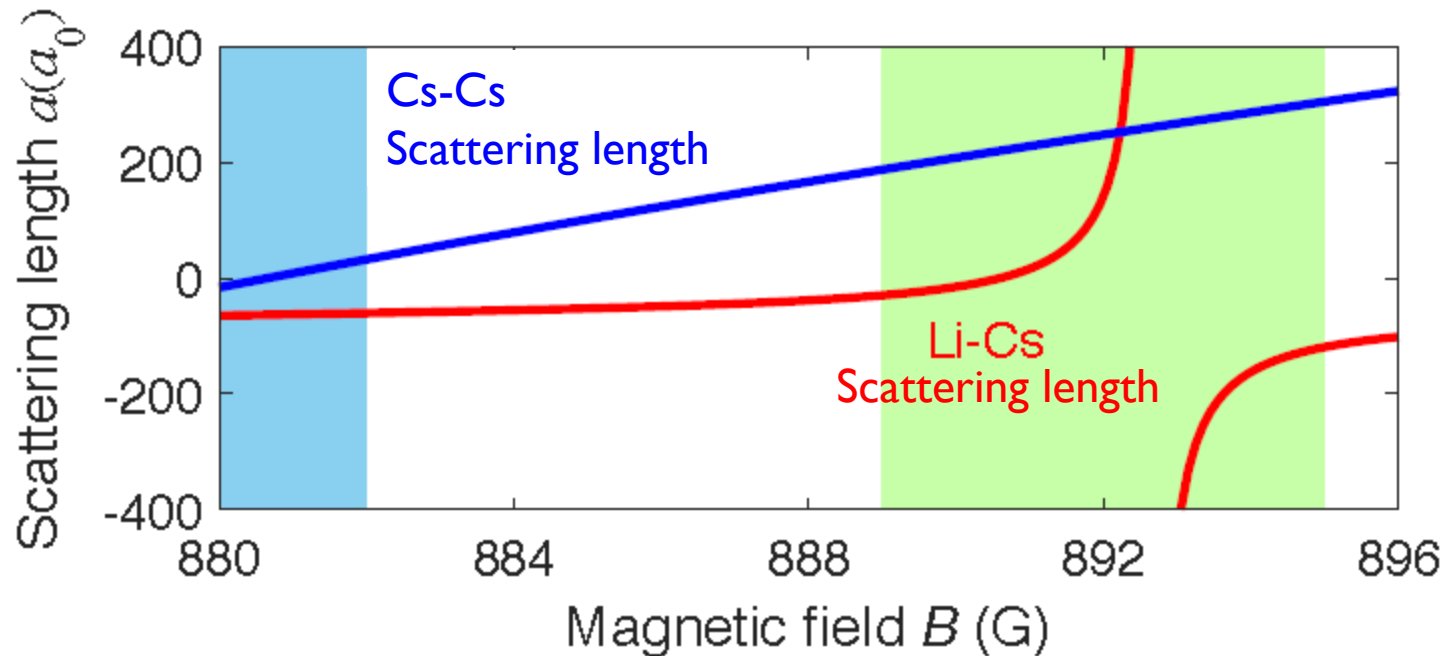
Superchemistry: Dynamics of Coupled Atomic and Molecular Bose-Einstein Condensates

D. Heinzen et al., PRL 84, 5029 (2000)

Molecular Matterwave Phase Doubling



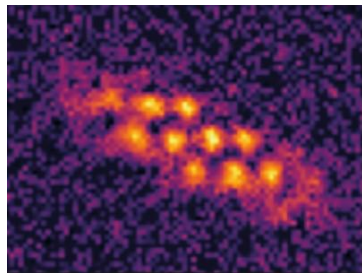
Lithium-Cesium Feshbach Resonance



Li-Cs Feshbach resonances (Chicago and Heidelberg): PRA '13,
Li-Cs₂ Efimov resonances: PRL '14 and '15 and Nature Physics 2017

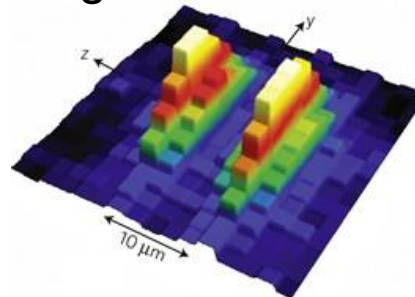
BEYOND CONTACT INTERACTIONS

Dipolar interactions



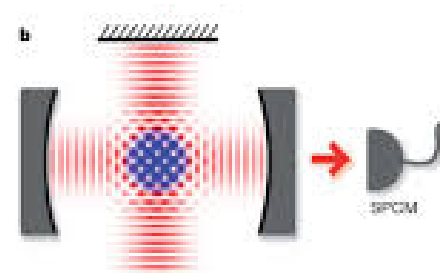
Cr (Stuttgart 2008)
Supersolid (LENS, UIUC and Innsbruck, 2019)
Molecules (JILA 2008, Columbia 2024)

Rydberg state



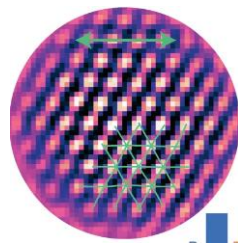
Blockade (Institut d'Optique, Wisconsin 2009)
Photon-photon interactions (MIT/Harvard 2012)
Molecular interactions (Stuttgart 2012)

Cavity induced interactions



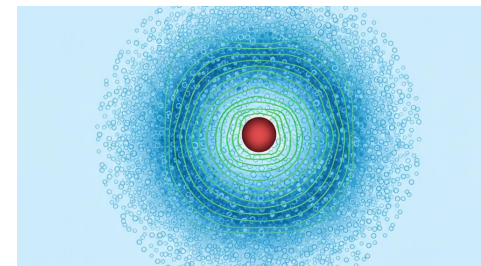
Collective cooling (MIT, MPQ 2003-)
Dicke transition (ETH, 2010)

Floquet Engineering



Lattice modulation (Chicago 2013-)
Interaction modulation (Chicago, Heidelberg, 2016-)

Fermion-mediated interactions

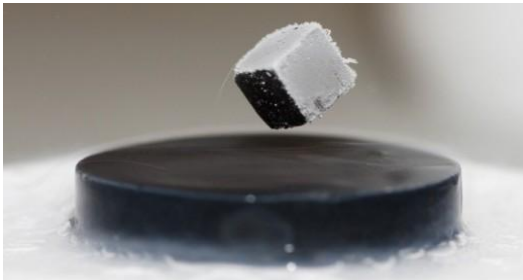
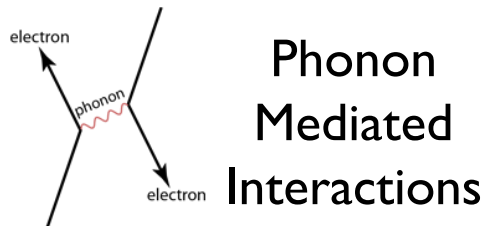


This talk

**Our
Experiments**

Mediated Interactions across Physics

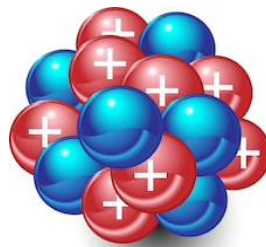
BCS pairing



Superconductivity

Yukawa Potential

Meson Mediated Interactions

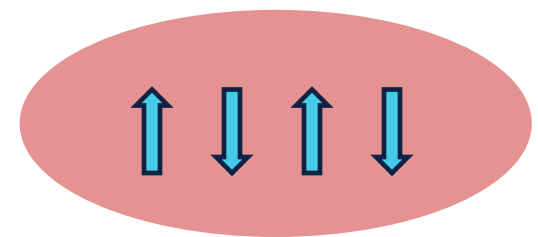


Atomic Nuclei

RKKY mechanism

Ruderman-Kittel-Kasuya-Yosida

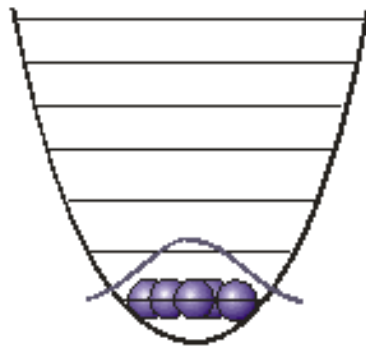
Fermion Mediated Interactions



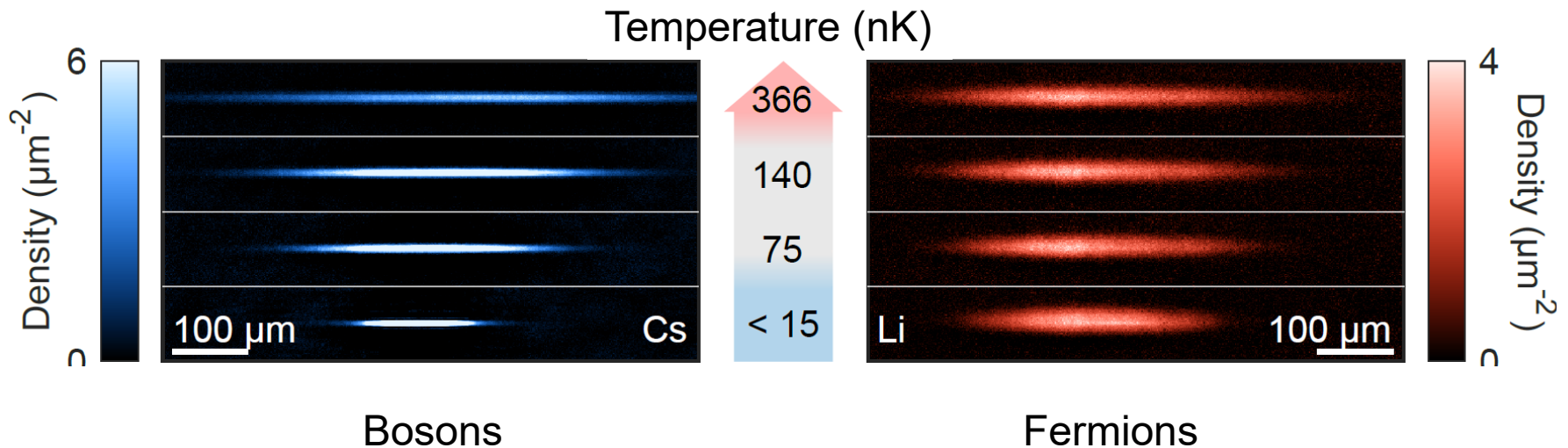
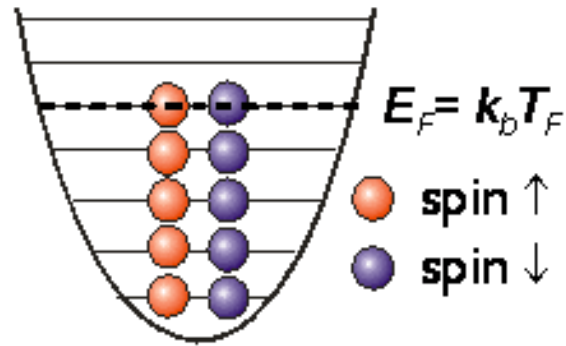
Magnetic Ordering

Atoms at low temperatures: Bosons Einstein condensate and degenerate Fermi gas

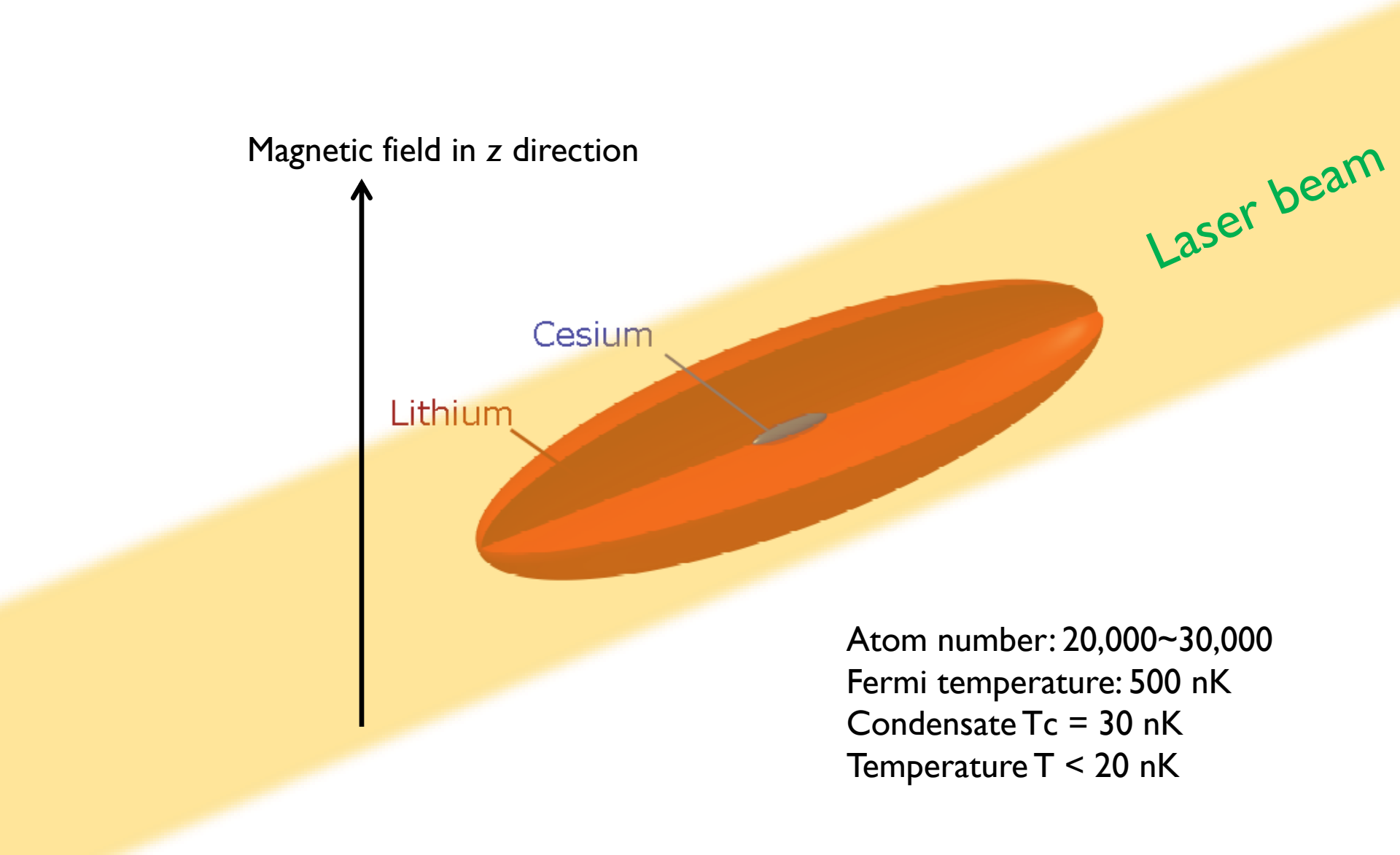
Bose-Einstein condensate



Degenerate Fermi gas



Degenerate quantum mixture of Cs133 and Li6



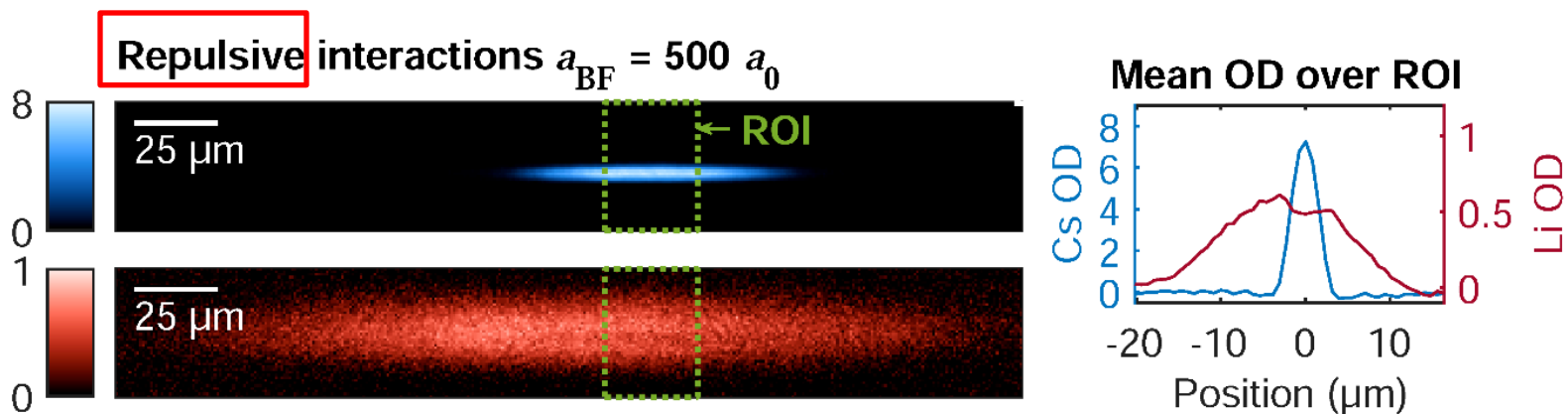
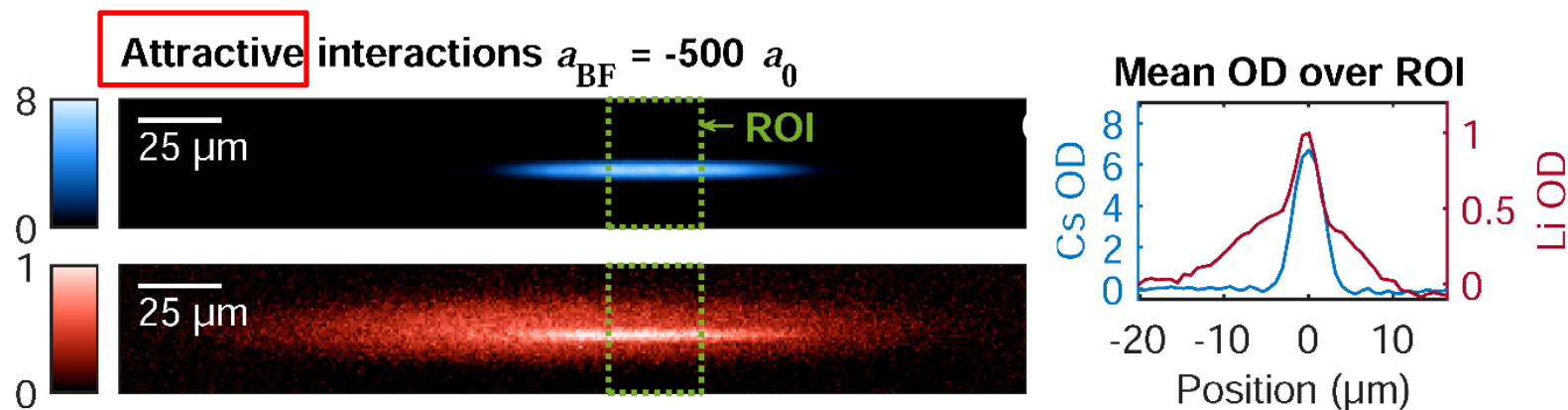
Atom number: 20,000~30,000

Fermi temperature: 500 nK

Condensate $T_c = 30$ nK

Temperature $T < 20$ nK

Simultaneous in situ imaging of Bose-Fermi mixture



Synopsis

RKKY – Efimov transition

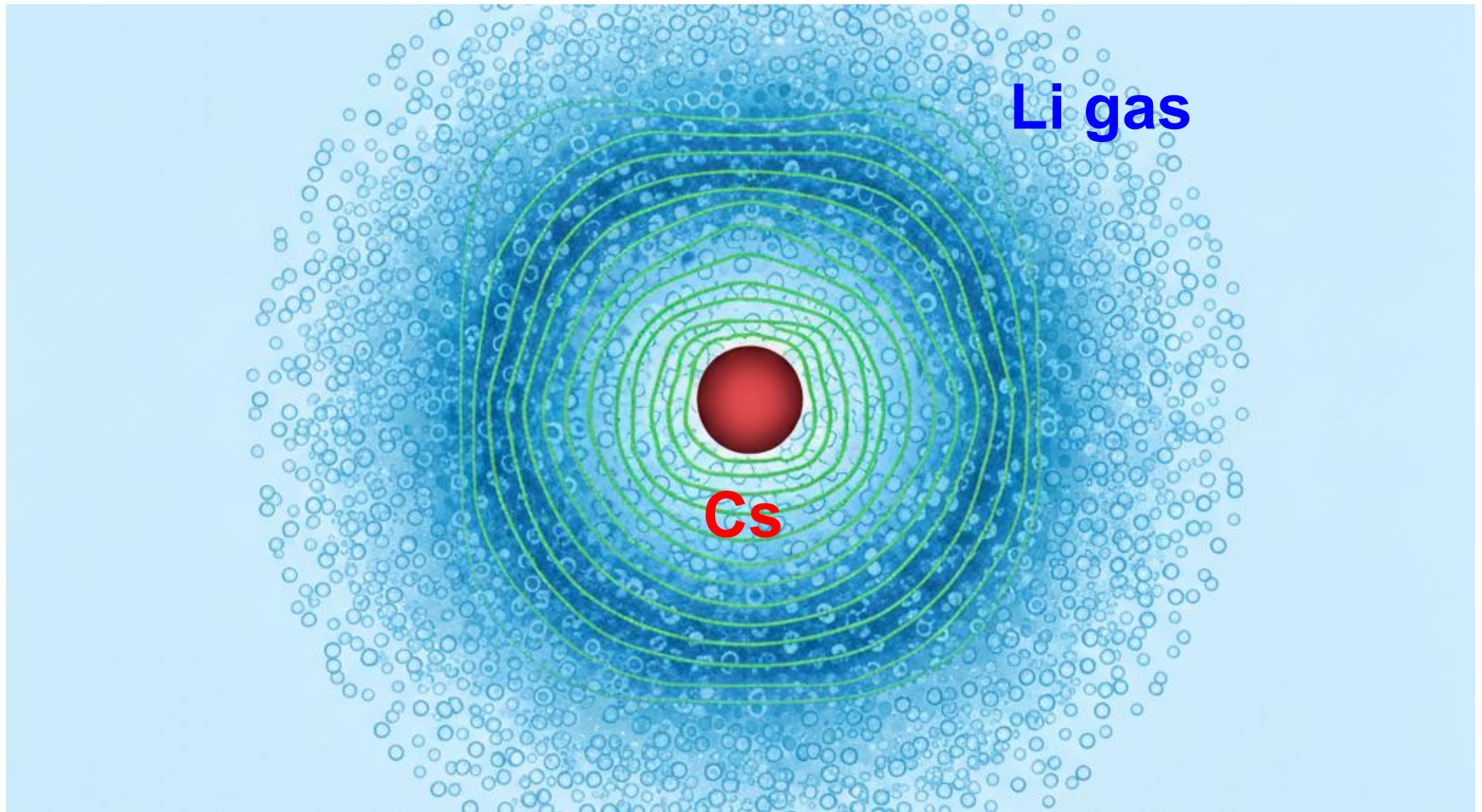
Heavy Boson-light Fermion mixture

Former experiments on Feshbach and Efimov resonances

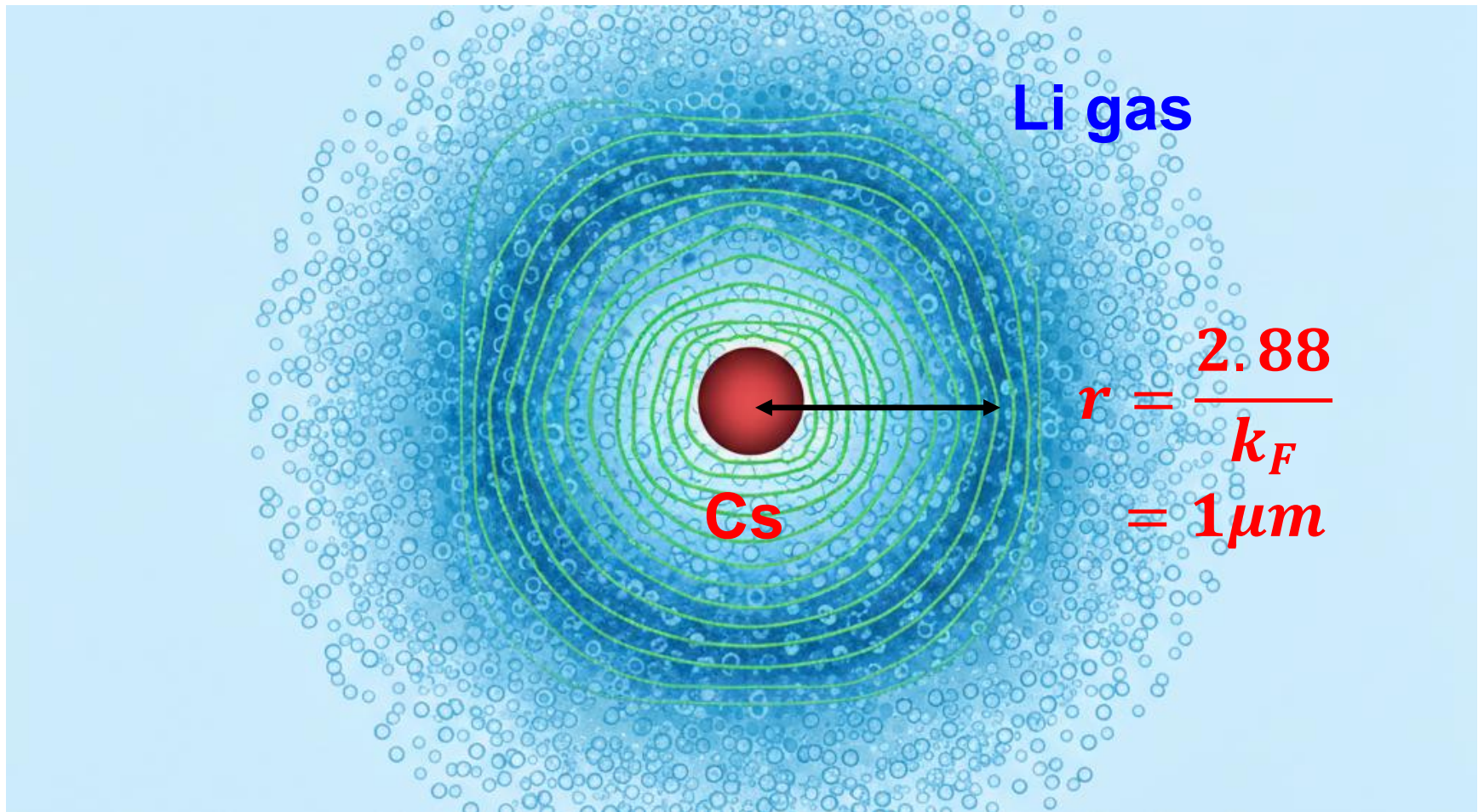
- *Equilibrium: Fermion mediated interactions*
- *Polaron to Polariton: Sound mode collapse and revival*
- *Strong coupling: Mediated scattering resonance*
- *Stability: Dispersion, heating and decay of BEC*

Physical picture

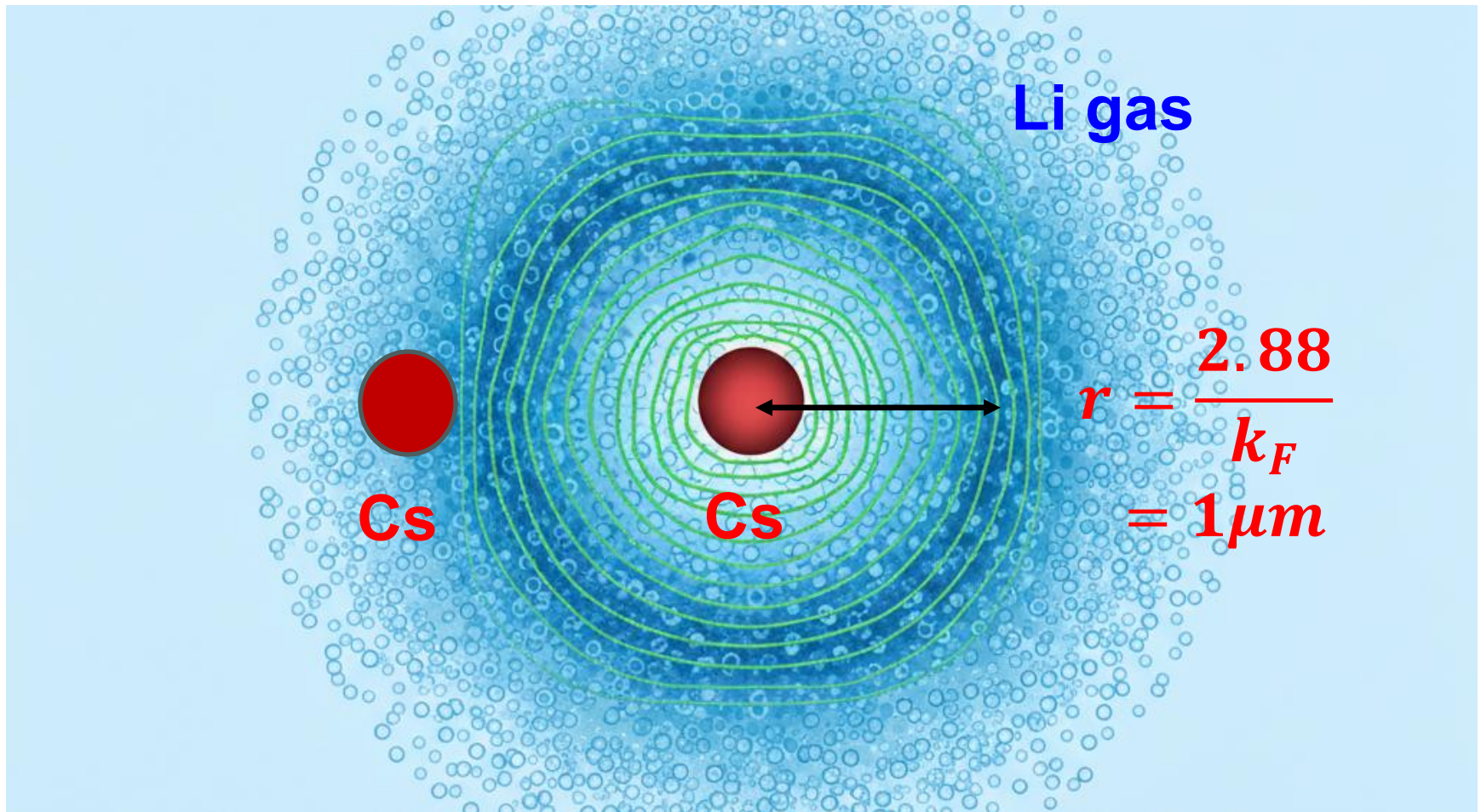
RKKY potential and Friedel oscillation



RKKY potential and Friedel oscillation

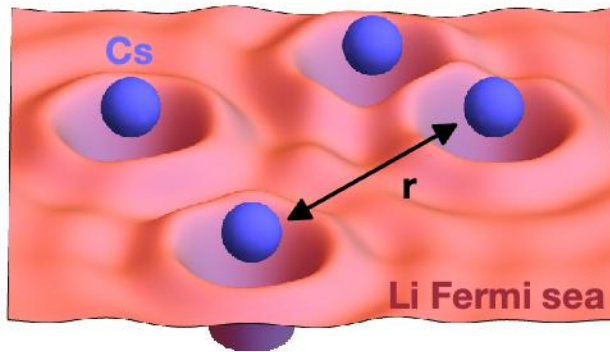


RKKY potential and Friedel oscillation



Mediated interactions in different regimes

Ruderman-Kittler-Kasuya-Yosida regime $|k_F a_{BF}| \ll 1$

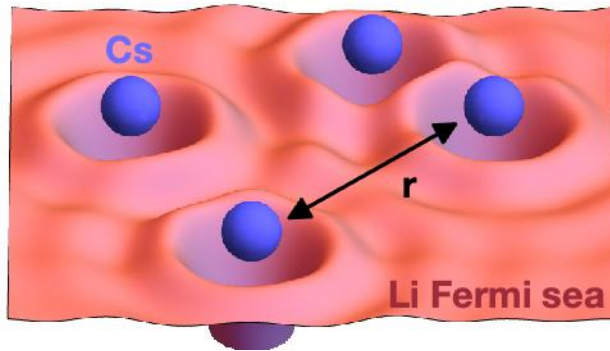


$$V_{RKKY}(r) = E_F \frac{8}{\pi} (k_F a_{BF})^2 \frac{R \cos R - \sin R}{R^4}$$

A graph showing the RKKY interaction potential $V_{RKKY}(r)$ as a function of $R = 2k_F r$. The vertical axis is labeled $V_{RKKY}(r)$ and the horizontal axis is labeled $R = 2k_F r$. The curve starts at a negative value, crosses the horizontal axis, reaches a positive peak, crosses the axis again, reaches a negative peak, and then oscillates with decreasing amplitude as R increases.

Mediated interactions in different regimes

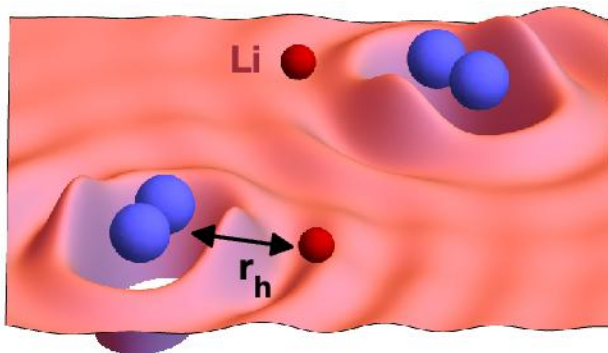
Ruderman-Kittler-Kasuya-Yosida regime $|k_F a_{BF}| \ll 1$



$$V_{RKKY}(r) = E_F \frac{8}{\pi} (k_F a_{BF})^2 \frac{R \cos R - \sin R}{R^4}$$

$R = 2k_F r$

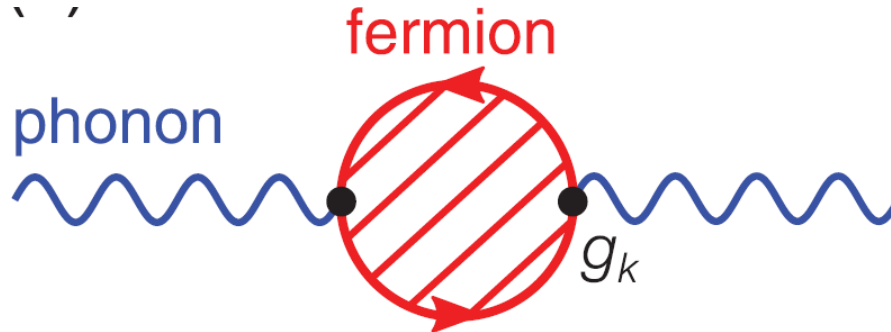
Efimov regime $|a_{BF}| \gg R_{vdW}$



$$V_{Efimov}(r) = -\frac{\hbar^2 \Theta(|a| - r)}{2m_r r^2}$$

r_H

From “Polaron” to “Polariton”



$$H = \sum_k \epsilon_k^F c_k^\dagger c_k + \sum_k \hbar \omega_k \alpha_k^\dagger \alpha_k + \sum_{k,q} g_k (\alpha_k + \alpha_{-k}^\dagger) c_q^\dagger c_{q-k}$$

Fermi energy
Phonon energy
Coupling

T. Enss and W. Zwerger, Eur. Phys. J. B 68, 383 (2009)

Compared with photons in solid

Conductor: $g_k \rightarrow \text{const.}$

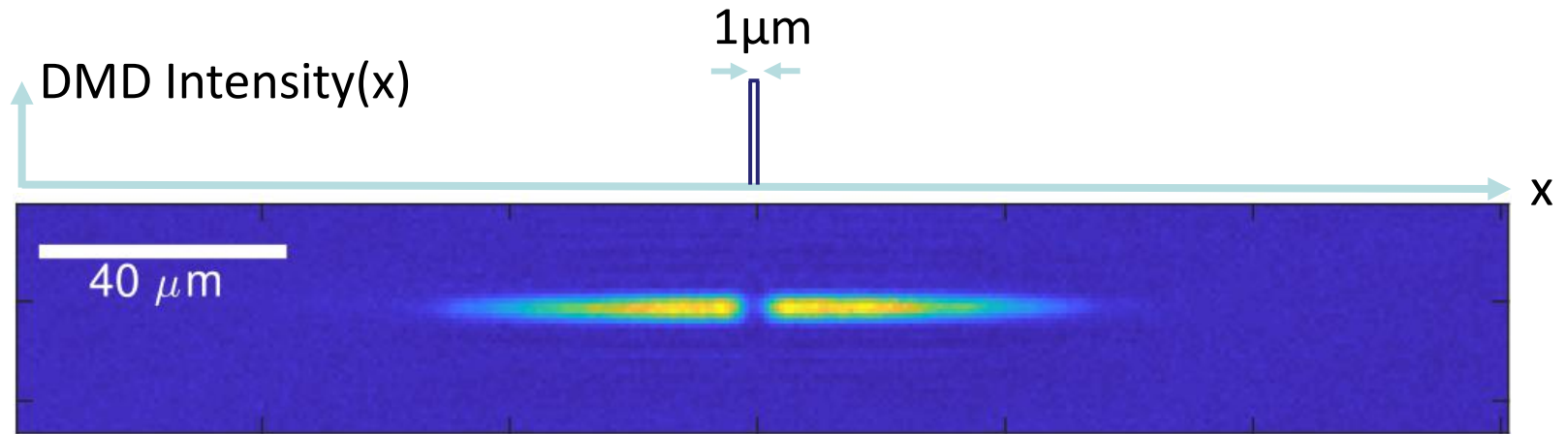
Insulator: $g_k \propto k$

BEC phonons in Fermi gas

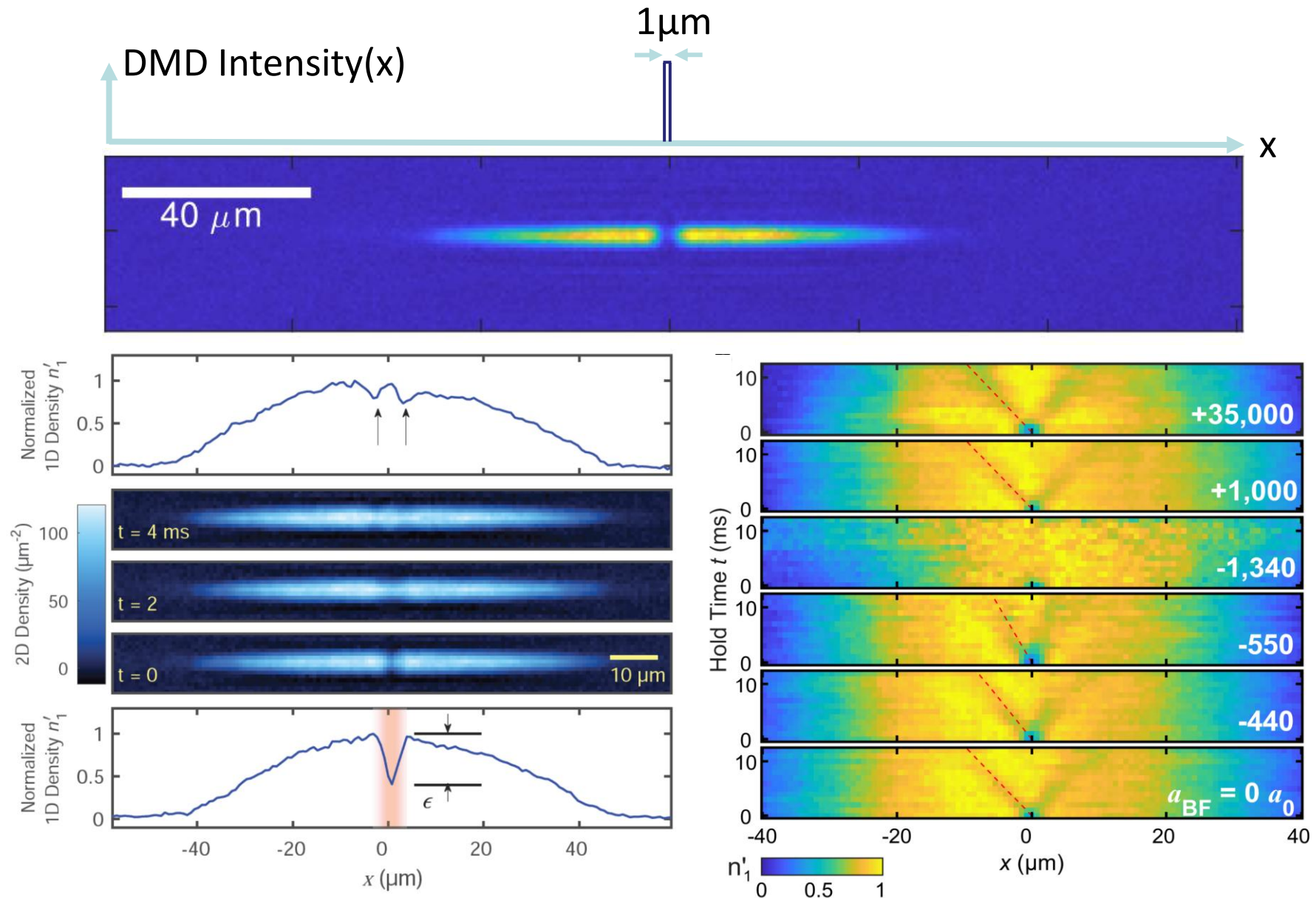
Gapless Fermi gas $g_k \propto k$

Gapped Fermi gas $g_k = o(k)$

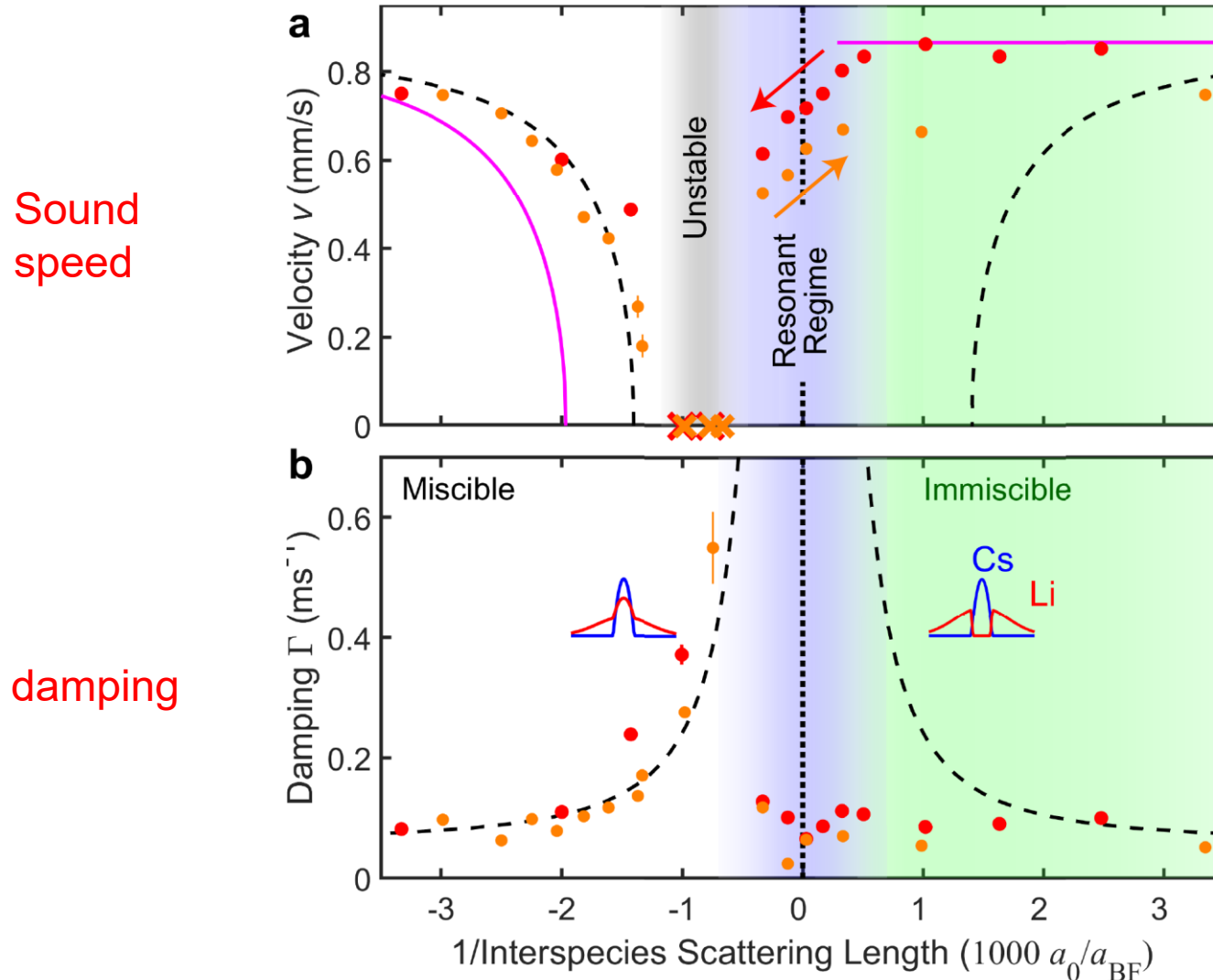
Sound propagation in Cs BEC



Sound propagation in Cs-Li mixture



Quench and revival of sound across propagation across the Feshbach resonance

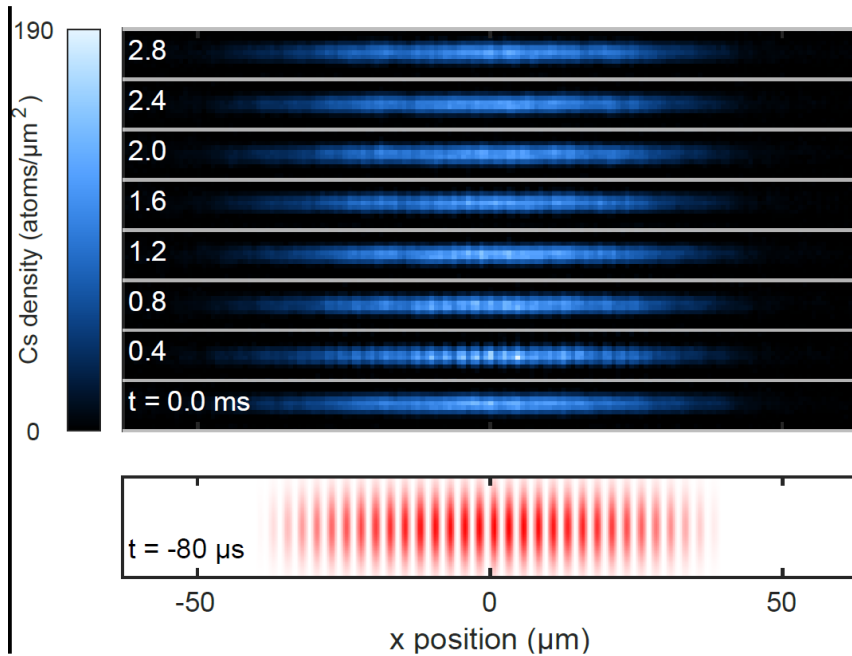


Observation of sound propagation in a strongly interacting Bose-Fermi mixture

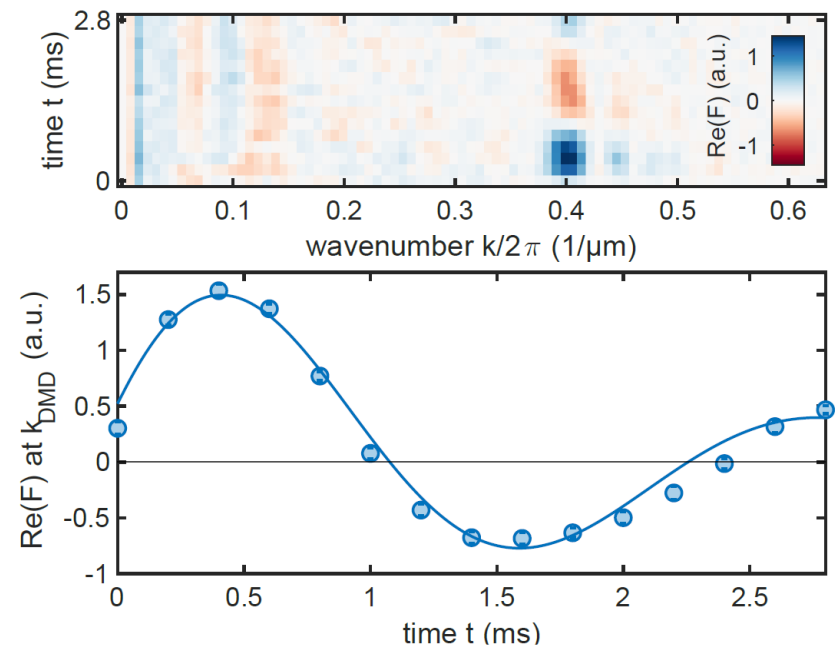
Krutik Patel, Geyue Cai, Henry Ando, Cheng Chin, [Phys. Rev. Lett. 131, 083003 \(2023\)](#)

Dispersion Measurement

Phase imprinting with a short pulse



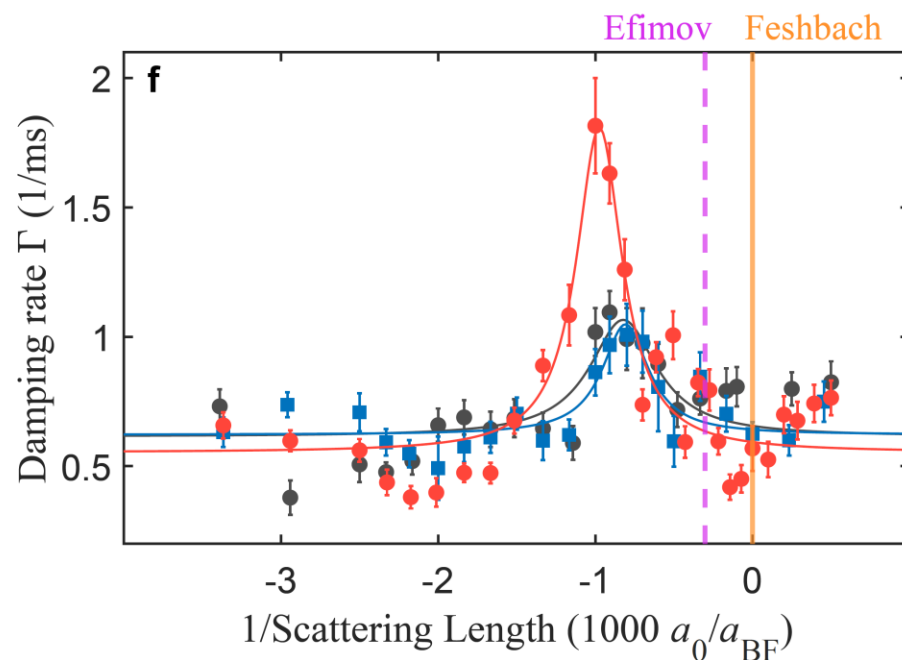
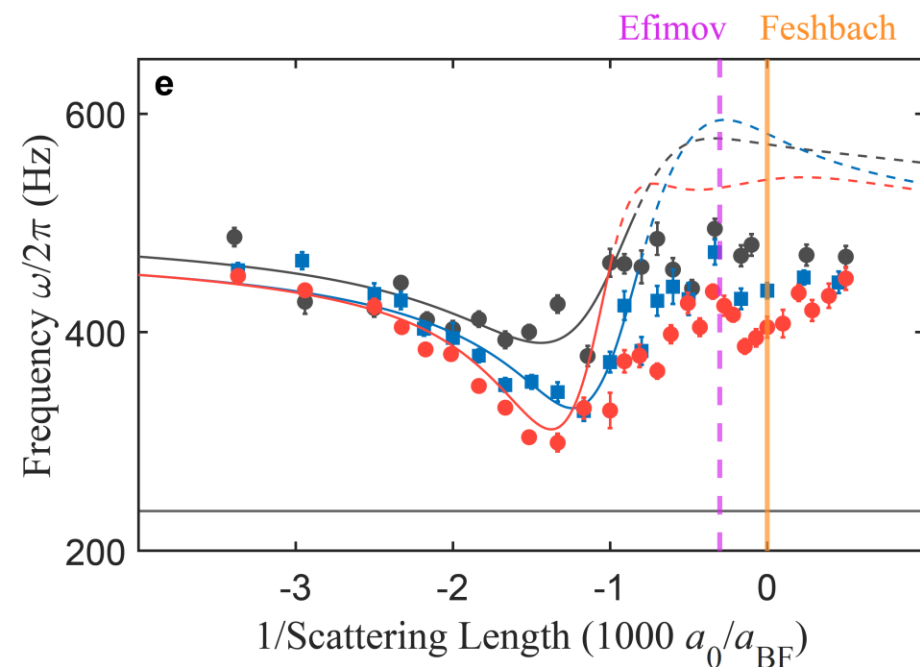
Density structure factor $S(k, t)$



Extract frequency ω and damping Γ

Dispersion of Mediated Interactions

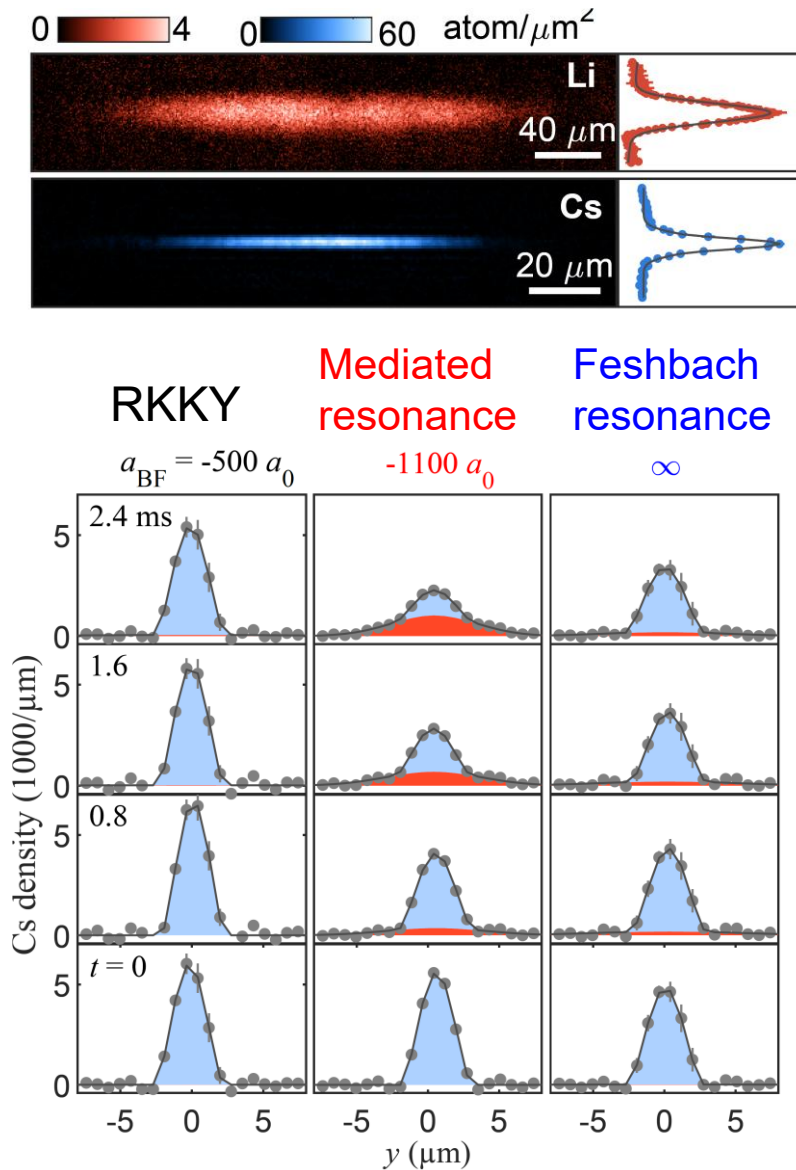
New mediated resonance!



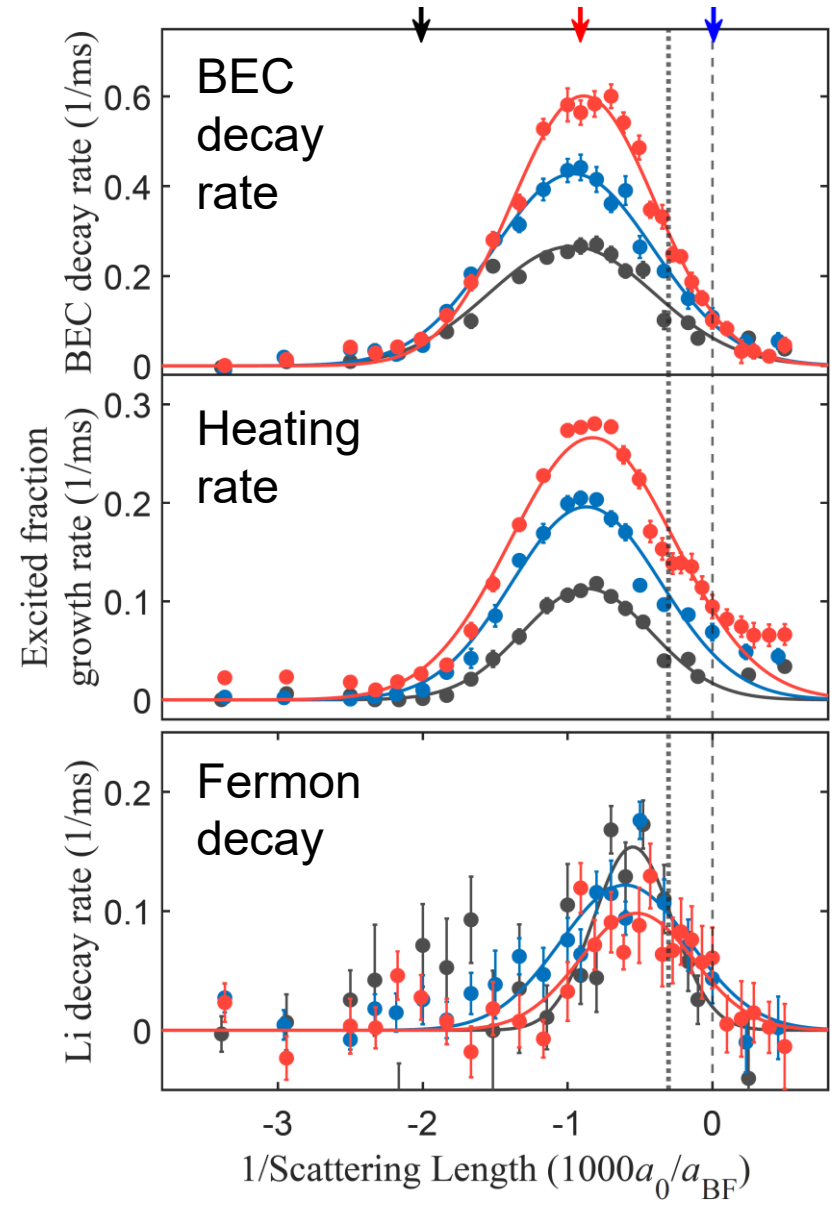
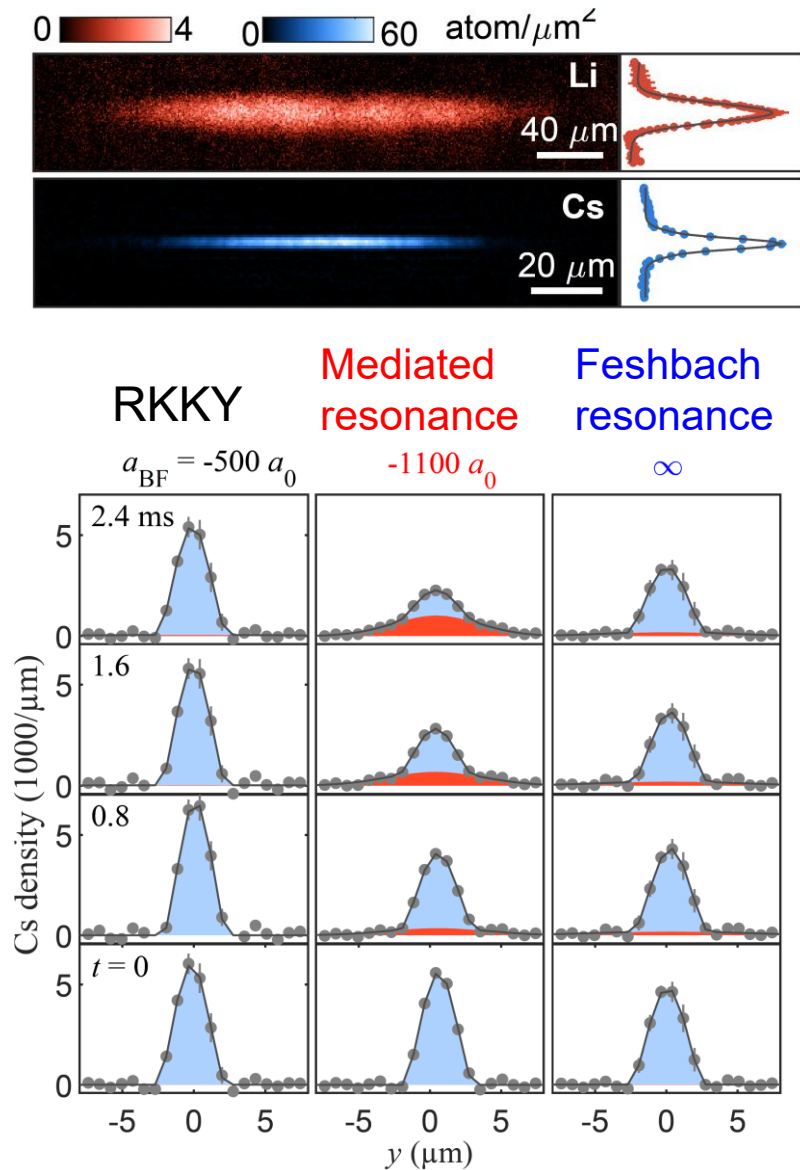
Fermion mediated pairing in the RKKY-Efimov transition regime
G. Cai, H. Ando, S. McCusker, C. C, PRL (2026)

Red: 100% Fermions
Blue: 50% Fermions
Black: 25% Fermions

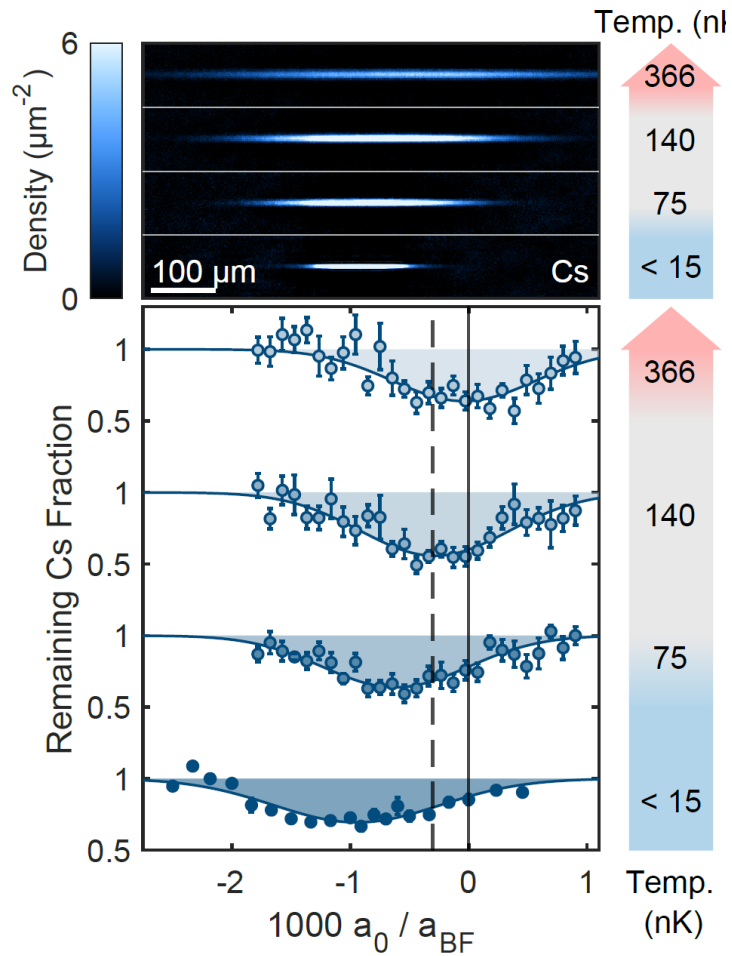
Damping and heating at mediated resonance



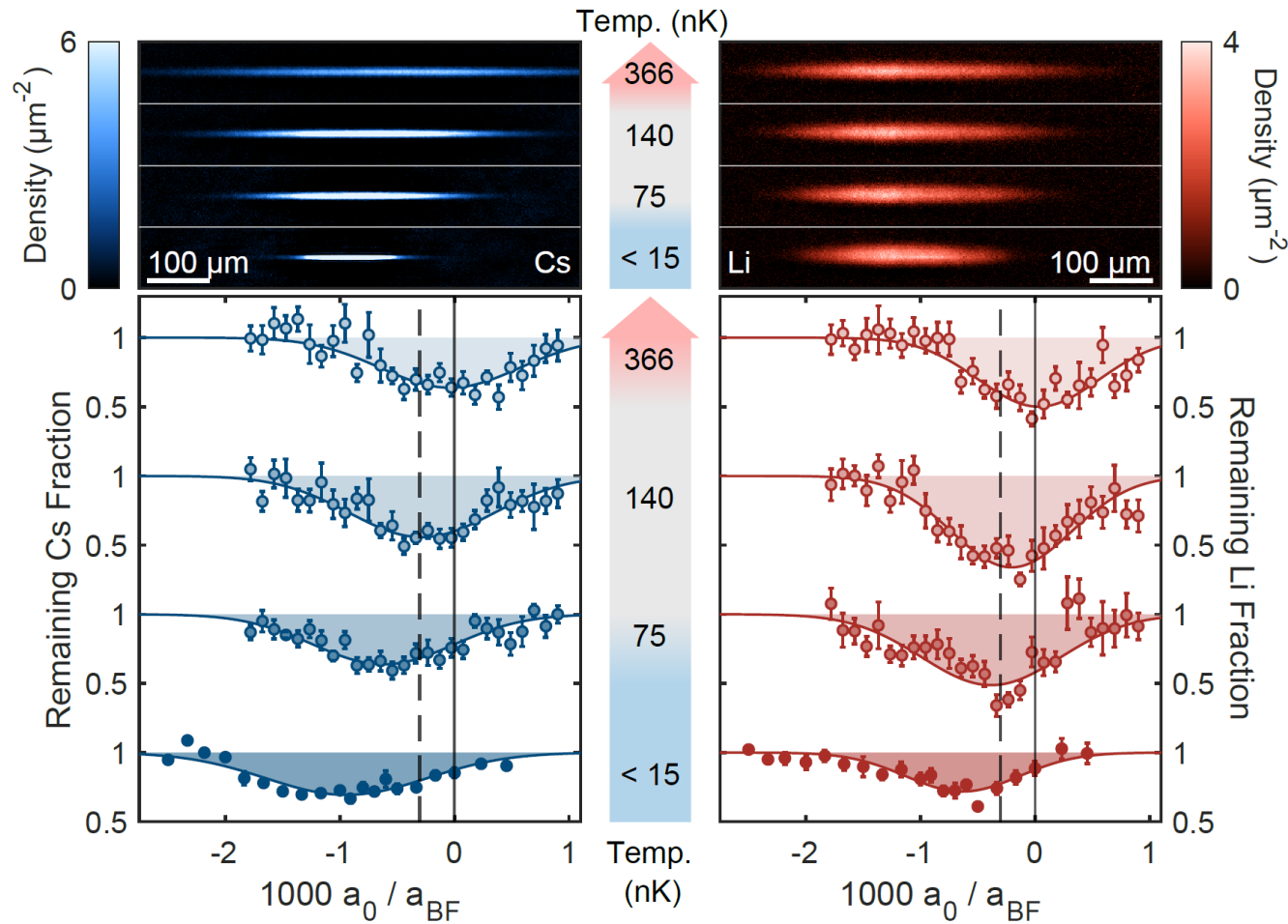
Damping and heating at mediated resonance



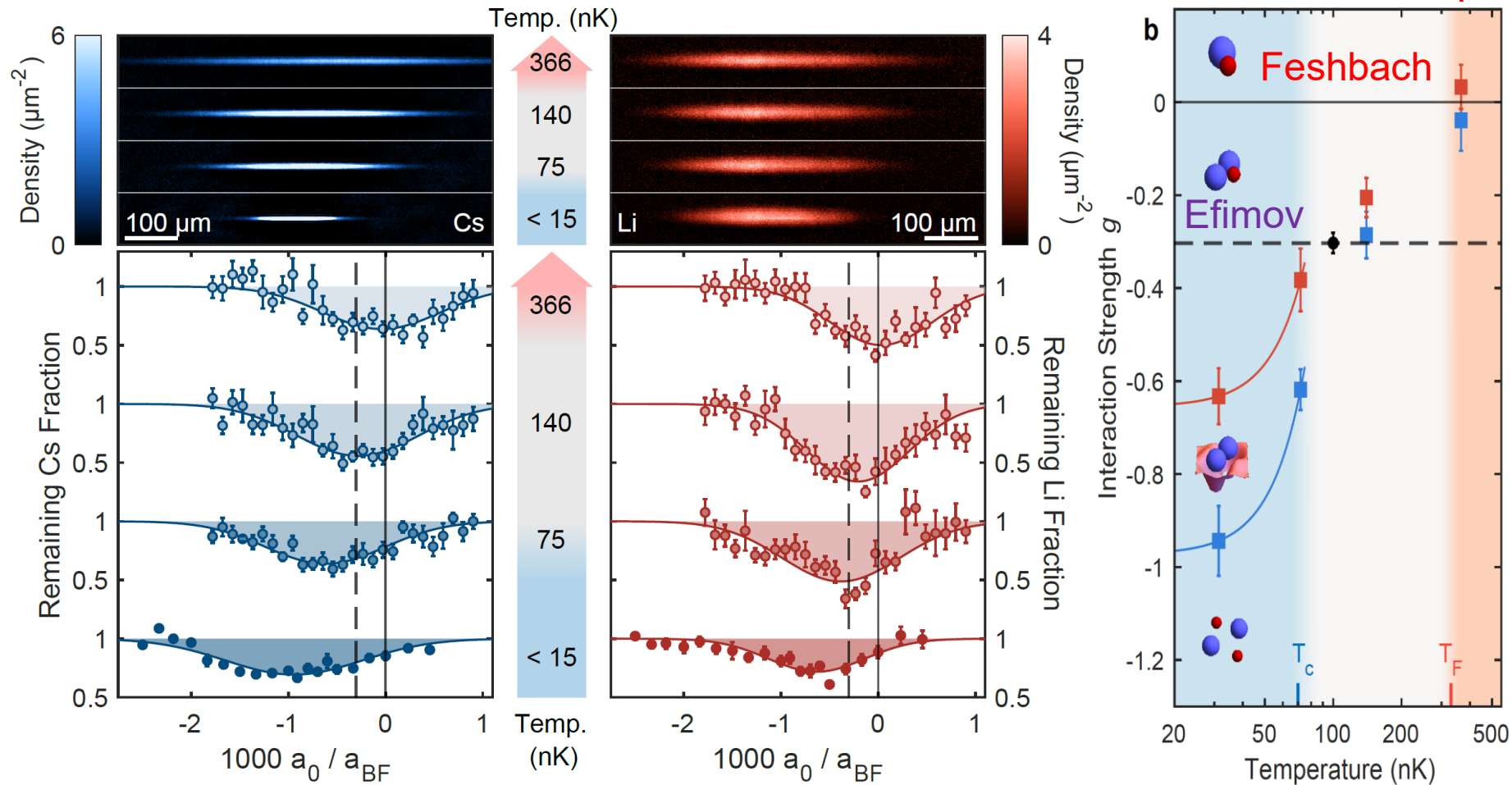
From thermal to quantum gas



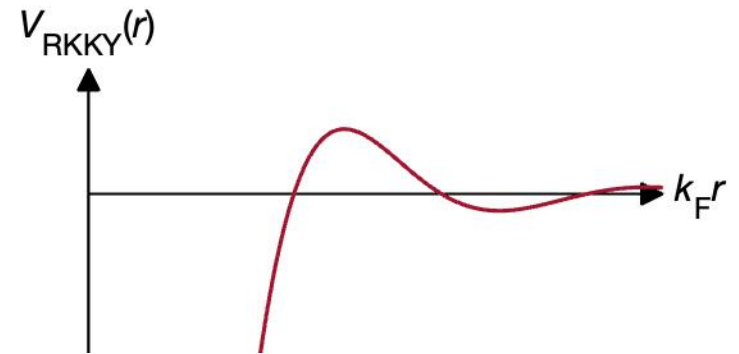
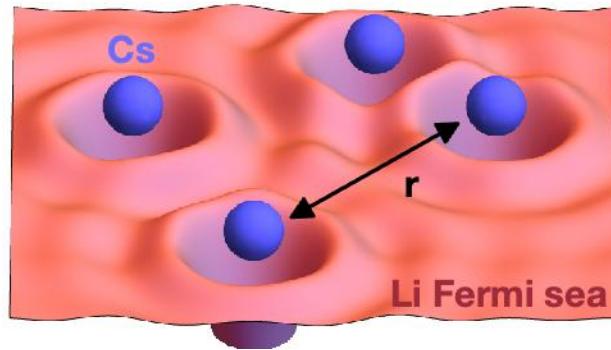
From thermal to quantum gas



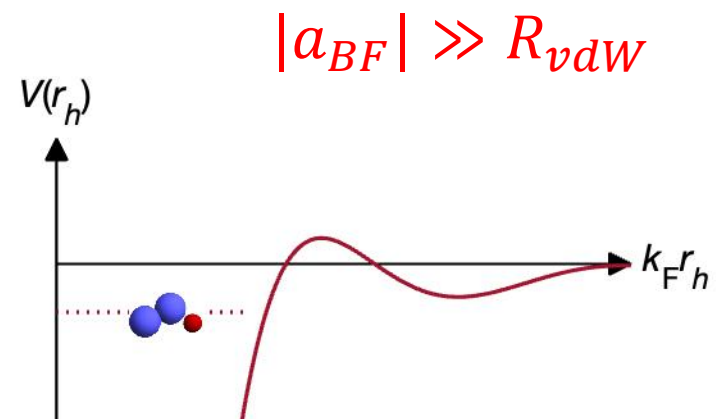
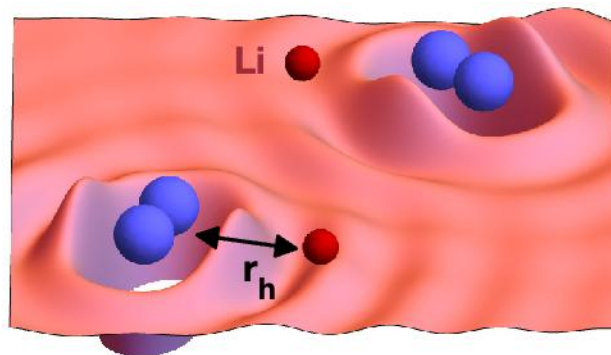
From thermal to quantum gas



Ruderman-Kittler-Kasuya-Yosida potential $|a_{BF}| \ll k_F^{-1}$



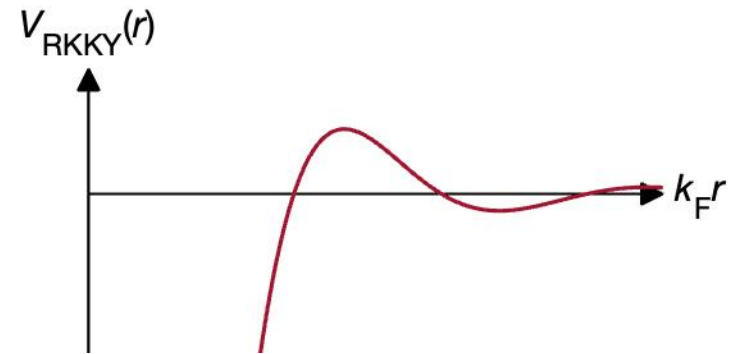
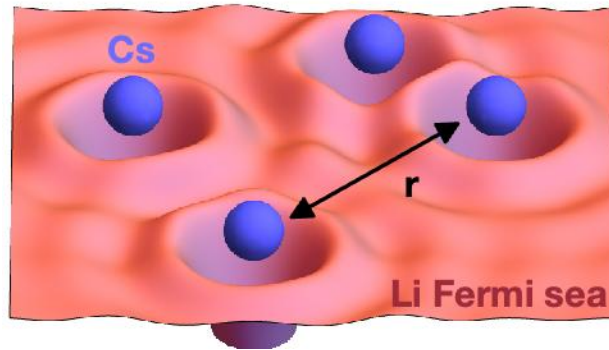
Efimov potential



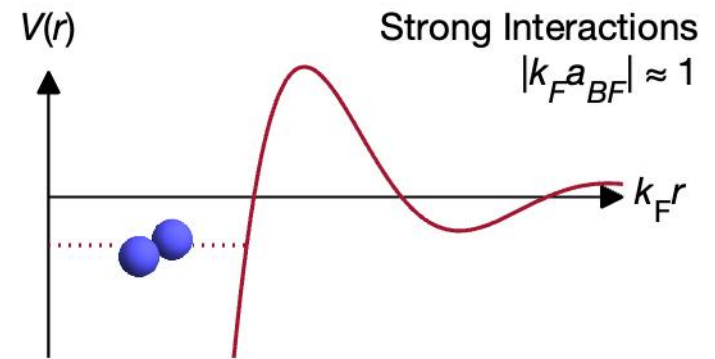
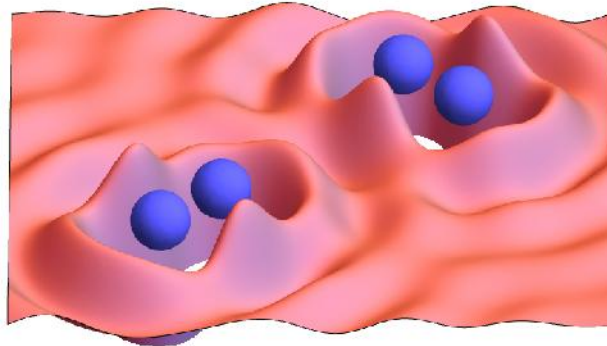
$$|a_{BF}| \gg R_{vdW}$$

Ruderman-Kittler-Kasuya-Yosida potential $|a_{BF}| \ll k_F^{-1}$

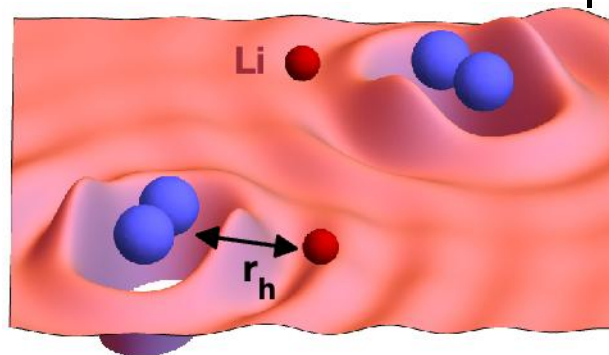
Attraction



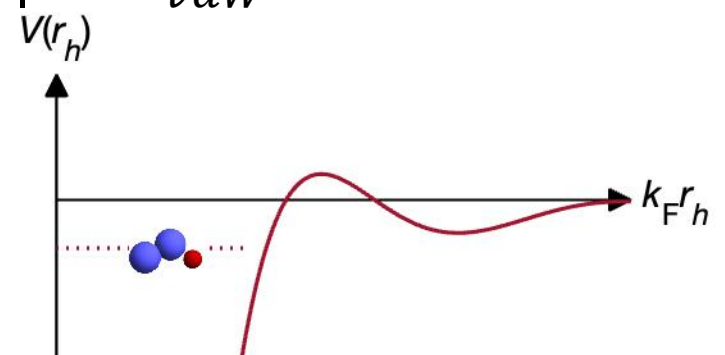
Fermion gas mediated pairing $|a_{BF}| \approx k_F^{-1}$



Efimov Cs₂Li trimer



$|a_{BF}| \gg R_{vdW}$



Conclusion

RKKY potential

- Fermion mediated interactions
- Quench of sound propagation

Fermion-mediated resonance

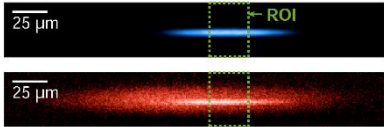
- Resonance in dispersion, damping, BEC decay at
Exp: $k_F a_{BF} = -0.51$

$$\text{Theory: } k_F \approx -\sqrt{\frac{m_F}{m_B} (2.5 + 3.1 k_F a_{BB})}$$

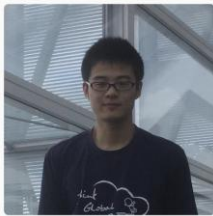
Efimov states

- LiCs2 three-body bound states

Acknowledgement



LiCs Team



Geyue Cai



Sarah
McCusker



Henry
Ando

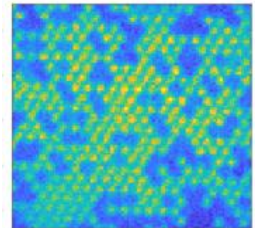
Theory



Tilman Enss
(Heidelberg)

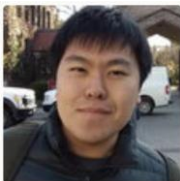


Michael
Rautenberg
(Heidelberg)



Cs BEC

Quantum Matter Synthesizer



Shu Nagata



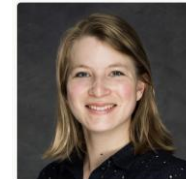
Dr. Tadej
Meznarsic



Lambert
Kong



Jiamei Zhang



Lauren Weiss



Evan
Yamaguchi